



basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

NATIONAL SENIOR CERTIFICATE

GRADE 12

MATHEMATICS P3

NOVEMBER 2010

MEMORANDUM

MARKS: 100

This memorandum consists of 15 pages.

NOTE:

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent Accuracy applies in ALL aspects of the marking memorandum.

QUESTION 1

<p>1.1</p>		<p>(7)</p>
<p>1.2</p>	<p> $5 + 12 + 2 + x + 75 - x + 66 - x + 3 + 2 = 103$ $x = 62$ </p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p>Note: Although CA applies to the question, the candidate cannot have negative or fraction answers.</p> </div>	<p> ✓ equation ✓ answer (2) </p>
<p>1.3.1</p>	<p> $P(\text{only eats chicken and fish and no vegetables}) = \frac{4}{103}$ </p>	<p> ✓ 4 ✓ 103 (2) </p>
<p>1.3.2</p>	<p> $P(\text{any two}) = \frac{12 + 4 + 13}{103} = \frac{29}{103}$ </p> <p>Accept</p> <p> $P(\text{any two}) = \frac{91}{103}$ </p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p>Note: Although CA applies to the question, the candidate cannot have negative or value greater than 1.</p> </div>	<p> ✓ adding probabilities ✓ $\frac{29}{103}$ (2) </p> <p> ✓ adding probabilities ✓ $\frac{91}{103}$ </p>

[13]

QUESTION 2

2.1	<p>No. They chose a Wednesday morning, when most people are at work. This is not a reliable time to do a survey about customer satisfaction. Most supermarkets are not busy at this time. Only 130 customers of a possible very large sample were interviewed. This is a very small number in comparison to the total number of customers that use a supermarket in a week.</p> <p>Accept: Yes, with a reasonable justification related to real life situations for example: very small rural community.</p> <p>Note: If the candidate answers YES or NO ONLY, then 0 / 2 marks.</p>	<p>No ✓✓ acceptable reason</p> <p>Yes ✓✓ acceptable reason</p> <p>(2)</p>
2.2	$\frac{22}{100} \times 130 = 28,6$ <p style="text-align: center;">OR</p> $\frac{78}{100} \times 130 = 101,4$ $130 - 101,4 = 28,6$ <p>Accept: 28 or 29</p>	<p>✓ $\frac{22}{100}$ or 22%</p> <p>✓ 28 or 29 or 28,6</p> <p>(2)</p>
2.3	<p>Choose a time when your store is busy, possibly Saturday or Sunday mornings. Interview more people to get a realistic point of view on customer service. Observe customer service over a longer period of time. Make use of questionnaires.</p> <p>Note: If yes in 2.1, the reasons must be relevant.</p>	<p>✓✓ any two valid reasons</p> <p>(2) [6]</p>

QUESTION 3

3.1	$\frac{68}{100} \times 20000$ $= 13\,600$ <p>OR</p> $\frac{66,7}{100} \times 20000$ $= 13\,340$ <p>OR</p> $\frac{68,3}{100} \times 20000$ $= 13\,660$	✓ 68 or 66,7 or 68,3 or $\frac{2}{3}$ ✓ answer (2)
3.2	<p>Lowest weight $= 182 - 3(0,454)$ $= 180,638$ grams Range $= 183,362 - 180,638$ $= 2,724$</p> <p>OR</p> $\text{Range} = 6 \times 0,454$ $= 2,724$ <p>Accept:</p> $\text{Range} = 8 \times 0,454$ $= 3,632$	<p>Highest Weight $= 182 + 3(0,454)$ $= 183,362$ grams</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p>Answer only: full marks</p> <p>If candidate uses one or two standard deviations: max 2 marks</p> </div> <p>✓ correct 3 sd ✓ lowest weight ✓ highest weight ✓ difference (4)</p> <p>✓✓ 6 ✓ 0,454 ✓ answer (4) [6]</p>

QUESTION 4

<p>4.1</p>	<p style="text-align: center;">Scatter plot showing resting heart rate vs heart rate after exercising</p> <table border="1" style="display: none;"> <caption>Data points from the scatter plot</caption> <thead> <tr> <th>Resting heart rate (beats per minute)</th> <th>Heart rate after jogging (beats per minute)</th> </tr> </thead> <tbody> <tr><td>47</td><td>65</td></tr> <tr><td>55</td><td>68</td></tr> <tr><td>62</td><td>80</td></tr> <tr><td>65</td><td>78</td></tr> <tr><td>68</td><td>75</td></tr> <tr><td>72</td><td>84</td></tr> <tr><td>75</td><td>81</td></tr> <tr><td>77</td><td>88</td></tr> <tr><td>79</td><td>90</td></tr> <tr><td>82</td><td>85</td></tr> <tr><td>83</td><td>105</td></tr> <tr><td>95</td><td>100</td></tr> </tbody> </table>	Resting heart rate (beats per minute)	Heart rate after jogging (beats per minute)	47	65	55	68	62	80	65	78	68	75	72	84	75	81	77	88	79	90	82	85	83	105	95	100	<p>✓✓✓ all 12 points plotted correctly</p> <p>✓✓ 7 – 11 points plotted correctly</p> <p>✓ 2 – 6 points plotted correctly</p> <p style="text-align: right;">(3)</p>
Resting heart rate (beats per minute)	Heart rate after jogging (beats per minute)																											
47	65																											
55	68																											
62	80																											
65	78																											
68	75																											
72	84																											
75	81																											
77	88																											
79	90																											
82	85																											
83	105																											
95	100																											
<p>4.2</p>	<p> $a = 25,23$ (25,22587269...) $b = 0,81$ (0,8143737166...) $\hat{y} = a + bx$ $\hat{y} = 25,23 + 0,81x$ </p> <p>If using pen and paper method: $\bar{x} = 71,25$ $\bar{y} = 83,25$ $a = 25,23$ (25,22587269...) $b = 0,81$ (0,8143737166...) $\hat{y} = a + bx$ $\hat{y} = 25,23 + 0,81x$ </p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p>Note: If the line of best fit is drawn and its equation then calculated: 0 / 4 marks</p> </div>	<p>✓✓ a or b ✓ b or a</p> <p>✓ $\hat{y} = 25,23 + 0,81x$ (4)</p> <p>✓ \bar{x}, \bar{y} ✓ a ✓ b</p> <p>✓ $\hat{y} = 25,23 + 0,81x$ (4)</p>																										
<p>4.3</p>	<p> $r = 0,898$ $= 0,90$ (0,8979098935...) </p>	<p>✓✓ answer (2)</p>																										
<p>4.4</p>	<p>It is a very strong positive relationship.</p>	<p>✓ strong ✓ positive (2)</p>																										
<p>4.5</p>	<p> $\hat{y} = 25,23 + 0,81x$ $86 = 25,23 + 0,81x$ $x = 75,024...$ Resting heart rate could be 75 beats per minute. </p> <p>If a and b are not rounded off in the calculation, $x = 74,626 ...$ $x = 74,63$ </p> <p>If candidate draws in the least square regression line and reads of x-value where $y = 86$: full marks</p>	<p>✓ substitute $\hat{y} = 86$</p> <p>✓ answer (2)</p> <p>Accept $x = 74,63$ [13]</p>																										

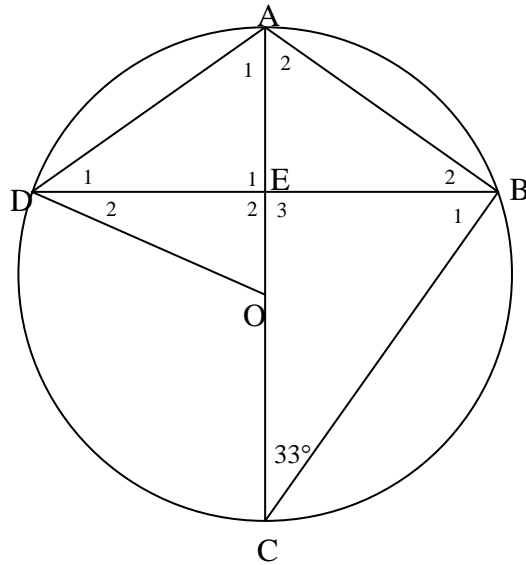
QUESTION 5

5.1	Number licence plates available $= 21 \times 21 \times 21 \times 10 \times 10 \times 10$ $= 21^3 \cdot 10^3$ $= 9\,261\,000$	✓ 21 ✓ 10 ✓ answer (3)
5.2	P(starting with Y) $= \frac{1 \times 21 \times 21 \times 10 \times 10 \times 10}{21 \times 21 \times 21 \times 10 \times 10 \times 10}$ $= \frac{441\,000}{9\,261\,000}$ $= \frac{1}{21}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;">Answer only: full marks</div>	✓ $21^2 \times 10^3$ ✓ denominator (CA with 5.1) ✓ answer (3)
5.3	P(contains number 7) $= \frac{21 \times 21 \times 21 \times 1 \times 9 \times 9 + 21 \times 21 \times 21 \times 9 \times 1 \times 9 + 21 \times 21 \times 21 \times 9 \times 9 \times 1}{9\,261\,000}$ $= \frac{3(21^3) \cdot 1.9.9}{9\,261\,000}$ $= \frac{243}{1000} \text{ or } 0,243$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;">If did not multiply by 3: max 2</div> <p>OR</p> P(contains number 7) $= \frac{1 \times 9 \times 9 + 9 \times 1 \times 9 + 9 \times 9 \times 1}{1000}$ $= \frac{243}{1000} \text{ or } 0,243$	✓ 3 ✓ 1.9.9 ✓ denominator (3) ✓ 3 or $1 \times 9 \times 9 + 9 \times 1 \times 9 + 9 \times 9 \times 1$ ✓ 1.9.9 ✓ denominator
5.4	Number of unique number plates available with no repetition $= 21 \times 20 \times 19 \times 10 \times 9 \times 8$ $= 5\,745\,600$ <p>OR</p> ${}^{21}P_3 \cdot {}^{10}P_3$ $= \frac{21!}{18!} \times \frac{10!}{7!}$ $= 5\,745\,600$	✓ $21 \times 20 \times 19$ ✓ $10 \times 9 \times 8$ ✓ answer (3) ✓ ${}^{21}P_3$ ✓ ${}^{10}P_3$ ✓ answer (3) [12]

QUESTION 6

<p>6.1</p>	<p> $T_1 = 3$ $T_{1+1} = 3 - 4(1) + 5 = 4$ $T_{2+1} = 4 - 4(2) + 5 = 1$ $T_{3+1} = 1 - 4(3) + 5 = -6$ </p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p>If 3 ; 0 ; - 7 ; - 18 : max 2 marks</p> </div>	<p> ✓ T_2 ✓ T_3 ✓ T_4 (3) </p>
<p>6.2</p>	<p> Quadratic sequence. It adds a linear sequence to the preceding term. OR </p> <div style="text-align: center; margin: 10px 0;"> </div> <p> Quadratic Sequence Constant second difference of - 4 OR Recursive Need the previous term to calculate the next term </p>	<p> ✓ quadratic ✓ reason (2) </p> <p> ✓ recursive ✓ reason (2) [5] </p>

QUESTION 7



<p>7.1</p>	<p>$\hat{D}_1 = 33^\circ$ (\angle in same segment) $\hat{A}ED = 90^\circ$ (given) $\hat{A}_1 = 57^\circ$ (\angle sum Δ)</p> <p>OR $\hat{B}EC = 90^\circ$ (given) $\hat{B}_1 = 57^\circ$ (\angle sum Δ) $\hat{A}_1 = 57^\circ$ (\angle in same segment)</p> <p>OR $DE = EB$ (line from circ cent \perp ch bis ch) AE is common $\hat{A}ED = \hat{E}_1 = 90^\circ$ (given) $\Delta AED \equiv \Delta AEB$ (SAS) $\hat{A}BC = 90^\circ$ (\angles in semi-circle) $\hat{A}_1 = \hat{A}_2 = 57^\circ$ (\angle sum Δ)</p>	<p>$\checkmark \hat{D}_1 = 33^\circ$ $\checkmark \angle$ in same segment $\checkmark \hat{A}_1 = 57^\circ$ (3)</p> <p>$\checkmark \hat{B}_1 = 57^\circ$ $\checkmark \hat{A}_1 = 57^\circ$ $\checkmark \angle$ in same segment (3)</p> <p>$\checkmark DE = EB$ (S/R)</p> <p>$\checkmark \Delta AED \equiv \Delta AEB$ (SAS)</p> <p>\checkmark answer (3)</p>
<p>7.2</p>	<p>$\hat{D}_2 + \hat{D}_1 = 57^\circ$ ($OD = OA =$ radii) $\hat{D}_2 = 24^\circ$</p> <p>OR $\hat{D}OC = 114^\circ$ ($OD = OA =$ radii) OR \angle at the centre theorem $\hat{E}_2 = 90^\circ$ $\hat{D}_2 = 114^\circ - 90^\circ$ $= 24^\circ$</p>	<p>$\checkmark \hat{D}_2 + \hat{D}_1 = 57^\circ$ \checkmark answer (2)</p> <p>$\checkmark \hat{D}OC = 114^\circ$</p> <p>$\checkmark$ answer (2)</p>

7.3	$\hat{A}BC = 90^\circ$ (\angle in semi-circle) $\hat{A}_2 = 57^\circ$ (\angle sum Δ) $= \hat{A}_1$ AE bisects $D\hat{A}B$ OR $DE = EB$ (line from circ centre bis ch) AE is common $\hat{E}_1 = \hat{A}EB = 90^\circ$ (given) $\Delta ADE \equiv \Delta ABE$ (SAS) $\hat{A}_2 = \hat{A}_1$	$\checkmark \hat{A}BC = 90^\circ$ $\checkmark \angle$ in semi-circle $\checkmark \hat{A}_2 = \hat{A}_1$ or AE bisects $D\hat{A}B$ (3) $\checkmark DE = EB$ (S/R) $\checkmark \Delta AED \equiv \Delta AEB$ (SAS) $\checkmark \hat{A}_2 = \hat{A}_1$ or AE bisects $D\hat{A}B$ (3) [8]
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QUESTION 8

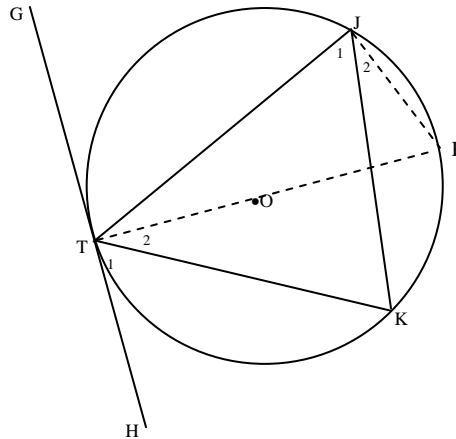
8.1 Draw diameter TP.
Join P to J.

$$\hat{T}_1 + \hat{T}_2 = 90^\circ \quad (\text{tan} \perp \text{diameter})$$

$$\hat{J}_1 + \hat{J}_2 = 90^\circ \quad (\angle \text{ in semi-circle})$$

$$\hat{J}_2 = \hat{T}_2 \quad (\angle \text{ in same seg})$$

$$\hat{TJK} = \hat{T}_1$$



- ✓ construction
 - ✓ $\hat{T}_1 + \hat{T}_2 = 90^\circ$
 - ✓ tan \perp diameter
 - ✓ S/R
 - ✓ S/R
- (5)

OR

Draw radii OT and OK

Let $\hat{T}_2 = x$

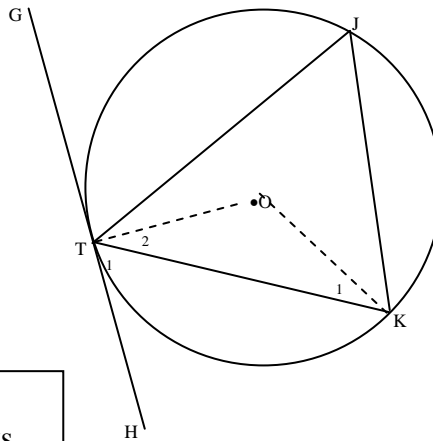
$$\hat{K}_1 = x \quad (\angle \text{ opp} = \text{ radii})$$

$$\hat{T}_1 = 90^\circ - x \quad (\text{rad} \perp \text{tan})$$

$$\hat{TOK} = 180^\circ - 2x \quad (\angle \text{ sum } \Delta)$$

$$\hat{TJK} = 90^\circ - x \quad (\angle \text{ circ cent})$$

$$\hat{TJK} = \hat{T}_1 \quad (= 90^\circ - x)$$

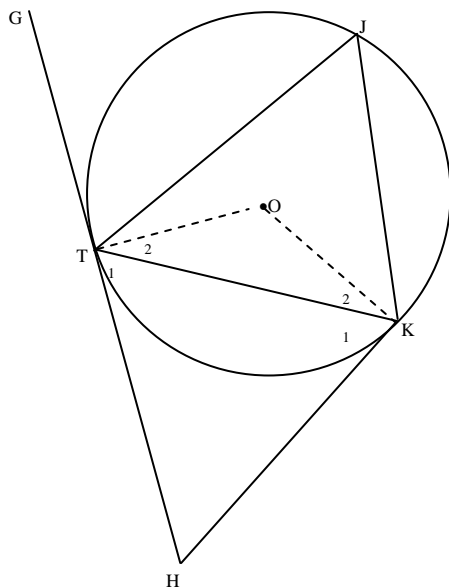


- ✓ construction
 - ✓ $\hat{T}_1 = 90^\circ - x$
 - ✓ rad \perp tan
 - ✓ S/R
 - ✓ S/R
- (5)

NOTE:

If there is no construction: 0 / 5 marks

If candidate changes lettering and states "Similarly": max full marks



OR

Draw GT extend to H. Draw tangent KH at K.

$$TH = KH \quad (\text{tan from comm pt})$$

$$\hat{K}_1 = \hat{T}_1 \quad (\angle s \text{ opp} = \text{sides})$$

$$\hat{TOK} = 2\hat{TJK}$$

$$(\angle \text{ circ cent} = 2\angle \text{ circumf})$$

$$\hat{T}_1 + \hat{T}_2 = 90^\circ \quad (\text{tan} \perp \text{radius})$$

$$\hat{TOK} = 180^\circ - (90^\circ - \hat{T}_1 + 90^\circ - \hat{K}_1)$$

$$= \hat{T}_1 + \hat{K}_1$$

$$= \hat{T}_1 + \hat{T}_1$$

$$= 2\hat{T}_1$$

$$\hat{T}_1 = \frac{1}{2} \hat{KOT}$$

$$= \hat{TJK}$$

- ✓ construction
 - ✓ S/R
 - ✓ S/R
 - ✓ $\hat{T}_1 + \hat{T}_2 = 90^\circ$
 - ✓ tan \perp radius
- (5)

OR

Construct OT, OJ and OK

$$\hat{T}_1 = \hat{J}_1 = x \quad (\text{radii})$$

$$\hat{T}_2 = \hat{K}_1 = z \quad (\text{radii})$$

$$\hat{K}_2 = \hat{J}_2 = y \quad (\text{radii})$$

$$2x + 2y + 2z = 180^\circ \quad (\angle \text{ sum } \Delta)$$

$$x + y + z = 90^\circ$$

$$x + y = 90^\circ - z$$

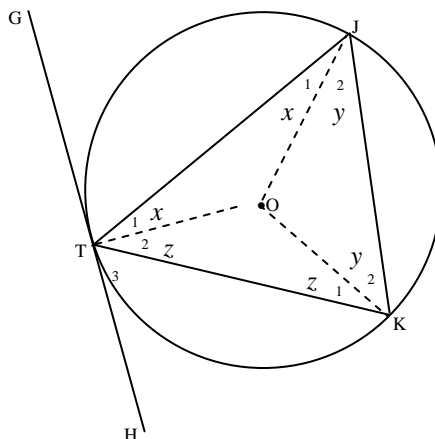
$$\hat{O}\hat{T}\hat{H} = 90^\circ \quad (\text{rad } \perp \text{ tan})$$

$$\hat{T}_3 = 90^\circ - z$$

$$= 90^\circ - (90^\circ - (x + y))$$

$$= 90^\circ - z$$

$$= \hat{T}\hat{J}\hat{K}$$



✓ construction
✓ S/R

✓ S

✓
 $\hat{T}_3 + \hat{T}_2 = 90^\circ$
✓ rad \perp tan

(5)

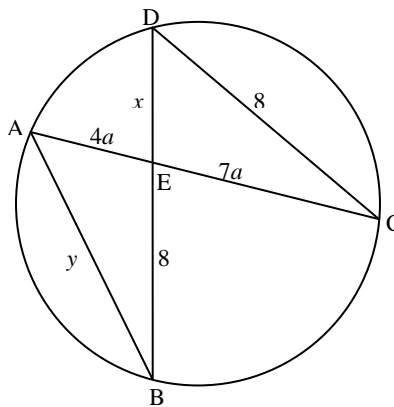
<p>8.2</p>		
<p>8.2.1</p>	<p>$\hat{B}_4 = x$ (tan chord theorem)</p> <p>$\hat{A} = \hat{B}_4 = x$ (corres \angle; $BD \parallel AO$)</p> <p>$\hat{B}_2 = x$ ($BO = EO = \text{radii}$)</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p>Note: If start with $\hat{A} = x$ and do not use tan ch th: max 2 marks</p> </div>	<p>✓ $\hat{B}_4 = x$</p> <p>✓ tan chord theorem</p> <p>✓ $\hat{A} = \hat{B}_4 = x$ with reason</p> <p>✓ $\hat{B}_2 = x$</p> <p style="text-align: right;">(4)</p>
<p>8.2.2</p>	<p>$\hat{DBE} = 90^\circ$ (\angle in semi-circle)</p> <p>$\hat{CBE} = 90^\circ + x$</p> <p>OR</p> <p>$\hat{CBO} = 90^\circ$ (rad \perp tan)</p> <p>$\hat{CBE} = 90^\circ + x$</p> <p>OR</p> <p>$\hat{O}_1 = 2x$ (\angle circ cent)</p> <p>$\hat{B}_3 = \hat{D}_1 = 90^\circ - x$ (radii)</p> <p>$\hat{CBE} = x + (90^\circ - x) + x = 90^\circ + x$</p>	<p>✓ $\hat{DBE} = 90^\circ$</p> <p>✓ \angle in semi-circle</p> <p>✓ $\hat{CBE} = 90^\circ + x$</p> <p style="text-align: right;">(3)</p> <p>✓ $\hat{CBO} = 90^\circ$</p> <p>✓ rad \perp tan</p> <p>✓ $\hat{CBE} = 90^\circ + x$</p> <p style="text-align: right;">(3)</p> <p>✓ $\hat{O}_1 = 2x$</p> <p>✓ \angle circ cent</p> <p>✓ $\hat{CBE} = 90^\circ + x$</p> <p style="text-align: right;">(3)</p>
<p>8.2.3</p>	<p>$\hat{DBE} = 90^\circ$ (proved in 8.2.2)</p> <p>$\hat{BFO} = 90^\circ$ (co-int angles supp; $BD \parallel AO$)</p> <p>$BF = FE$ (line from circ cent \perp ch bisect ch)</p> <p>F is the midpoint of EB</p>	<p>✓ $\hat{DBE} = 90^\circ$</p> <p>✓ $\hat{BFO} = 90^\circ$ and reason</p> <p>✓ $BF = FE$</p> <p>✓ line from circ cent \perp ch bisect ch)</p> <p style="text-align: right;">(4)</p>

	<p>OR $OD = OE$ (radii) $BF = FE$ ($BD \parallel AO$) F is the midpoint of EB</p> <p>OR $\hat{BFO} = \hat{EFO} = 90^\circ$ ($BD \parallel AO$) OF is common $BO = OE$ (radii) $\triangle BOF \equiv \triangle EOF$ (90°HS) $BF = FE$ ($\equiv \triangle$s)</p> <p>OR $\hat{B}_2 = \hat{A} = x$ (proven) \hat{O}_2 is common $\triangle AOB \parallel \triangle BOF$ (AAA) $\hat{A}BO = \hat{B}FO$ $\hat{A}BO = 90^\circ$ (proven) $\hat{A}BO = \hat{B}FO = 90^\circ$ $BF = FE$ (line from circ cent \perp ch bisects ch)</p> <p>OR $\hat{D}BE = 90^\circ$ (\angle in semi-circle) $\hat{B}_3 = 90^\circ - x$ $\hat{O}_2 = 90^\circ - x$ (alt \angles; $BD \parallel FO$) $\hat{F}_1 = 90^\circ$ (\angle sum \triangle) $BF = FE$ (line from circ cent \perp ch bisects ch)</p> <p>OR In $\triangle OBF$ and $\triangle OEF$ 1. $OB = OE$ (radii) 2. $\hat{BFO} = \hat{EFO} = 90^\circ$ ($BD \parallel AO$) 3. $\hat{B}_2 = \hat{E}$ (radii) $\triangle OBF \equiv \triangle OEF$ (AAS) $BF = FE$</p>	<p>✓ $OD = OE$ ✓ radii ✓ $BF = FE$ ✓ $BD \parallel AO$ (4)</p> <p>✓ $\hat{BFO} = \hat{EFO} = 90^\circ$ ($BD \parallel AO$) ✓ $BO = OE$ ✓ $\triangle BOF \equiv \triangle EOF$ ✓ $BF = FE$ (4)</p> <p>✓ $\triangle AOB \parallel \triangle BOF$ ✓ $\hat{A}BO = \hat{B}FO$ ✓ $BF = FE$ ✓ line from circ cent \perp ch bisects ch (4)</p> <p>✓ $\hat{D}BE = 90^\circ$ ✓ $\hat{F}_1 = 90^\circ$ ✓ $BF = FE$ ✓ line from circ cent \perp ch bisects ch (4)</p> <p>✓ $OB = OE$ ✓ $\hat{BFO} = \hat{EFO} = 90^\circ$ ($BD \parallel AO$) ✓ $\triangle OBF \equiv \triangle OEF$ ✓ $BF = FE$ (4)</p>
<p>8.2.4</p>	<p>In $\triangle CBD$ and $\triangle CEB$ 1. $\hat{E} = \hat{B}_4 = x$ (proven in 8.2.1) 2. \hat{C} is common 3. $\hat{D}_4 = \hat{C}BE = 90^\circ + x$ $\triangle CBD \parallel \triangle CEB$ (AAA)</p>	<p>✓ $\hat{E} = \hat{B}_4 = x$ ✓ \hat{C} is common Or ✓ $\hat{D}_4 = \hat{C}BE = 90^\circ + x$ Any two of the above (2)</p>

8.2.5	$\frac{EB}{BD} = \frac{CE}{CB}$ (sim Δ s \therefore sides in proportion) $EB \cdot CB = CE \cdot BD$ but $EB = 2EF$ (F is the midpoint of BE) $2EF \cdot CB = CE \cdot BD$	$\checkmark \frac{EB}{BD} = \frac{CE}{CB}$ $\checkmark EB \cdot CB = CE \cdot BD$ $\checkmark EB = 2EF$ (3) [21]
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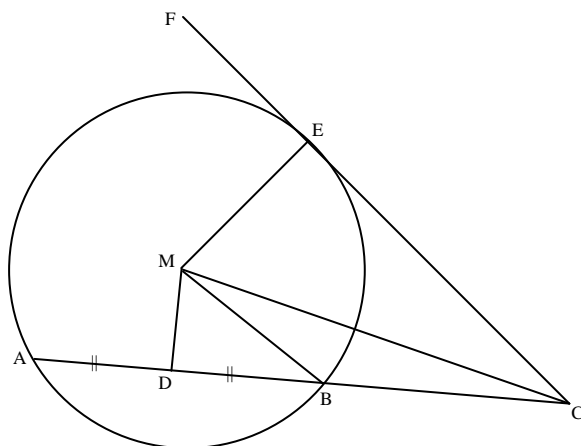
QUESTION 9

9.	$\hat{A} = \hat{D}$ (\angle in same seg) $\hat{B} = \hat{C}$ (\angle in same seg) $\hat{AEB} = \hat{DEC}$ (vert opp \angle s) $\Delta DEC \parallel \Delta AEB$ ($\angle \angle \angle$) $\frac{DE}{AE} = \frac{EC}{EB} = \frac{DC}{AB}$ (sides in prop) Let $AC = 11a$ $\frac{x}{4a} = \frac{7a}{8}$ $x = \frac{28a^2}{8}$ $x = 3,5a^2$ $\frac{y}{8} = \frac{8}{7a}$ (sides in prop) $y = \frac{64}{7a}$	$\checkmark \hat{A} = \hat{D}$ S/R $\checkmark \hat{B} = \hat{C}$ S/R $\checkmark \hat{AEB} = \hat{DEC}$ $\checkmark \checkmark \checkmark \Delta DEC \parallel \Delta AEB$ ($\angle \angle \angle$) [6]
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If candidate proves similarity of two triangles: full marks.
 If candidate does not prove similarity max 3 marks. The triangles have to be in the correct order in order to be given 3 marks.

QUESTION 10



<p>10.1</p>	<p> $\hat{M}EC = 90^\circ$ (tan \perp rad) $\hat{M}DC = 90^\circ$ (line from cent bisects ch) $\hat{M}EC + \hat{M}DC = 180^\circ$ $\therefore MDCE$ a cyclic quad (opp \angles of quad supplementary) </p> <p>OR</p> <p> $\hat{M}EC = 90^\circ$ (tan \perp rad) $\hat{M}DA = 90^\circ$ (line from cent bisects ch) $\hat{M}EC = \hat{M}DA$ $\therefore MDCE$ a cyclic quad (ext \angle quad = int opp) </p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p>NOTE: If the word <i>cyclic</i> is used in the last reason: max 2 / 3 marks</p> </div>	<p> ✓ $\hat{M}EC = 90^\circ$ (tan \perp rad) ✓ $\hat{M}DC = 90^\circ$ ✓ opp \angles of quad supplementary (3) ✓ $\hat{M}EC = 90^\circ$ (tan \perp rad) ✓ $\hat{M}DA = 90^\circ$ ✓ ext \angle quad = int opp (3) </p>
<p>10.2</p>	<p> $MD^2 = MB^2 - DB^2$ (Pythagoras; ΔMBD) $MC^2 = MD^2 + DC^2$ (Pythagoras; ΔMDC) $= MB^2 - DB^2 + DC^2$ </p>	<p> ✓ $MD^2 = MB^2 - DB^2$ ✓ Pythagoras ✓ $MC^2 = MD^2 + DC^2$ (3) </p>
<p>10.3</p>	<p> $DB = 30$ (given) $MB = 40$ (radii) $MC^2 = (40)^2 + (50)^2 - (30)^2$ $= 3\ 200$ $MC = 40\sqrt{2} = 56,57$ $MC^2 = ME^2 + CE^2$ (Pythagoras) $CE^2 = 3\ 200 - 1\ 600$ $CE^2 = 1\ 600$ $CE = 40$ mm </p> <p>OR</p> <p> $MC^2 = CE^2 + ME^2 - 2CE \cdot ME \cdot \cos \hat{M}EC$ $3200 = CE^2 + (40)^2 - 2CE \cdot (40) \cdot \cos 90^\circ$ $= CE^2 + 1600$ $CE^2 = 1600$ $CE = 40$ </p>	<p> ✓ $MB = ME$ ✓ $DB = 30$ ✓ $MC^2 = 3200$ or $MC = 40\sqrt{2}$ or $MC = 56,57$ </p> <p> ✓ answer (4) </p> <p> ✓ cosine rule ✓ $ME = 40$ ✓ $MC^2 = 3200$ </p> <p> ✓ answer (4) </p> <p style="text-align: right;">[10]</p>

TOTAL: 100